ME2025 Digital Control

Some Useful Summations

Jee-Hwan Ryu

School of Mechanical Engineering Korea University of Technology and Education

Some Useful Summations

Geometric Progression

$$\sum_{i=0}^{\infty} a^i = \frac{1}{1-a}$$

|a| < 1

Some Useful Summations

Finite Geometric Summation

$$\sum_{i=0}^{N} a^{i} = \begin{cases} 0 & if \quad a = 0\\ N+1 & if \quad a = 1\\ \frac{1-a^{N+1}}{1-a} & otherwise \end{cases}$$

Derive from #1

Note: no restriction on value of a

Some Useful Summations

$$\sum_{i=0}^{\infty} ia^i = \frac{a}{\left(1-a\right)^2}$$

|a| < 1

Some Useful Summations

$$\sum_{i=0}^{N} i = \frac{N(N+1)}{2}$$

$$e^x = \sum_{i=0}^{\infty} \frac{x^i}{i!}$$

Exponential series